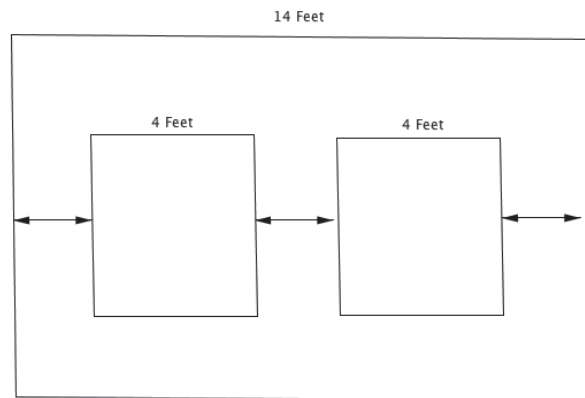


Lesson 7: Understanding Equations

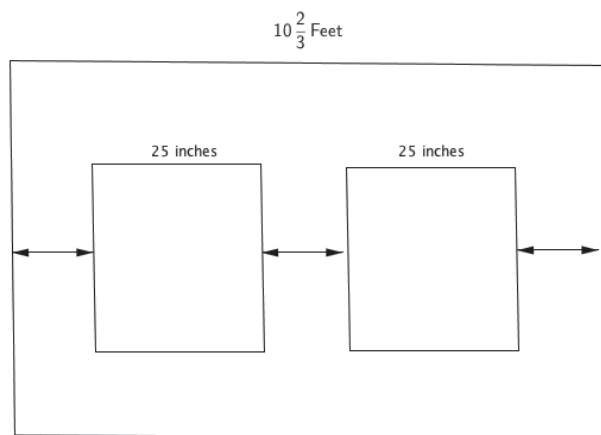
Classwork

Opening Exercise

Your brother is going away to college, so you no longer have to share a bedroom. You decide to redecorate a wall by hanging two new posters on the wall. The wall is 14 feet wide and each poster is four feet wide. You want to place the posters on the wall so that the distance from the edge of each poster to the nearest edge of the wall is the same as the distance between the posters, as shown in the diagram below. Determine that distance.



Your parents are redecorating the dining room and want to place two rectangular wall sconce lights that are 25 inches wide along a $10\frac{2}{3}$ foot wall so that the distance between the lights and the distances from each light to the nearest edge of the wall are all the same. Design the wall and determine the distance.



Let the distance between a light and the nearest edge of a wall be x ft. Write an expression in terms of x for the total length of the wall. Then, use the expression and the length of the wall given in the problem to write an equation that can be used to find that distance.

Now write an equation where y stands for the number of *inches*: Let the distance between a light and the nearest edge of a wall be y inches. Write an expression in terms of y for the total length of the wall. Then, use the expression and the length of the wall to write an equation that can be used to find that distance (in inches).

What value(s) of y makes the second equation true: 24, 25, or 26?

Exercise

Sophia pays a \$19.99 membership fee for an online music store.

- a. If she also buys two songs from a new album at a price of \$0.99 each, what is the total cost?

- b. If Sophia purchases n songs for \$0.99 each, write an expression for the total cost.

- c. Sophia's friend has saved \$118 but is not sure how many songs she can afford if she buys the membership and some songs. Use the expression in part (b) to write an equation that can be used to determine how many songs Sophia's friend can buy.

- d. Using the equation written in part (c), can Sophia's friend buy 101, 100, or 99 songs?

Relevant Vocabulary

VARIABLE (DESCRIPTION): A *variable* is a symbol (such as a letter) that represents a number (i.e., it is a placeholder for a number).

EQUATION: An *equation* is a statement of equality between two expressions.

NUMBER SENTENCE: A *number sentence* is a statement of equality between two numerical expressions.

SOLUTION: A *solution* to an equation with one variable is a number that, when substituted for the variable in both expressions, makes the equation a true number sentence.

Lesson Summary

In many word problems, an equation is often formed by setting an expression equal to a number. To build the expression, it is helpful to consider a few numerical calculations with just numbers first. For example, if a pound of apples costs \$2, then three pounds cost \$6 (2×3), four pounds cost \$8 (2×4), and n pounds cost $2n$ dollars. If we had \$15 to spend on apples and wanted to know how many pounds we could buy, we can use the expression $2n$ to write an equation, $2n = 15$, which can then be used to find the answer: $7\frac{1}{2}$ pounds.

To determine if a number is a solution to an equation, substitute the number into the equation for the variable (letter) and check to see if the resulting number sentence is true. If it is true, then the number is a solution to the equation. For example, $7\frac{1}{2}$ is a solution to $2n = 15$ because $2\left(7\frac{1}{2}\right) = 15$.

Problem Set

1. Check whether the given value is a solution to the equation.

a. $4n - 3 = -2n + 9$ $n = 2$

b. $9m - 19 = 3m + 1$ $m = \frac{10}{3}$

c. $3(y + 8) = 2y - 6$ $y = 30$

2. Tell whether each number is a solution to the problem modeled by the following equation.

Mystery Number: Five more than -8 times a number is 29. What is the number?

Let the mystery number be represented by n .

The equation is $5 + (-8)n = 29$.

- Is 3 a solution to the equation? Why or why not?
 - Is -4 a solution to the equation? Why or why not?
 - Is -3 a solution to the equation? Why or why not?
 - What is the mystery number?
3. The sum of three consecutive integers is 36.
- Find the smallest integer using a tape diagram.
 - Let n represent the smallest integer. Write an equation that can be used to find the smallest integer.
 - Determine if each value of n below is a solution to the equation in part (b).

$$n = 12.5$$

$$n = 12$$

$$n = 11$$

4. Andrew is trying to create a number puzzle for his younger sister to solve. He challenges his sister to find the mystery number. “When 4 is subtracted from half of a number the result is 5.” The equation to represent the mystery number is $\frac{1}{2}m - 4 = 5$. Andrew’s sister tries to guess the mystery number.
- Her first guess is 30. Is she correct? Why or why not?
 - Her second guess is 2. Is she correct? Why or why not?
 - Her final guess is $4\frac{1}{2}$. Is she correct? Why or why not?